

Integrity checking for combined databases

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Description of the problem

- ICs are properties of the DB that must always hold
- The integrity must be checked wrt the ICs after every update (typically tested in an *ad hoc* way at the application level)
- In a data integration system, it's the same
- Idea: generate specialized versions of the ICs to be automatically executed
 - For expected kinds of updates
 - Assuming the integrity before the update
 - Generalize this technique to data integration systems

A simplification framework

1. Produce a **weakest precondition**

Ex: $\varphi = \leftarrow p(x) \qquad U = p(a)$
 $\text{After}^U(\varphi) = \leftarrow (p(x) \vee x = a)$

A condition about the updated state that can be checked in the present state

2. Use the fact that φ was known to hold before the update (Cond. Weak. Prec.).
3. Take the weakest CWP.

DEF: $\text{Simp}^U(\varphi) = \text{Weaken}_{\varphi}(\text{After}^U(\varphi))$

A simplification framework - Example

$$\varphi = \leftarrow m(x, y) \wedge m(x, z) \wedge y \neq z$$

checked by posing it as a query against the DB
and expecting an empty answer

$$U = m(\text{Bob}, \text{Alice})$$

$$\text{simp}^U(\varphi) = \leftarrow m(\text{Bob}, y) \wedge y \neq \text{Alice}$$

Mappings

- Mapping = a way to associate n local DBs to a global DB
- GaV mapping = the global DB is expressed as a set of views over the local sources.
- LaV mapping = the local DBs are expressed as a set of views over the global DB.
- We assume:
 - sound mappings (the views produce only but not necessarily all correct information)
 - no existential quantifier in LaV mappings
 - $\Rightarrow$ LaV mappings can be rewritten as GaV mappings without skolemization

Mappings - example

LaV mapping $L =$

$$\{ m_1(x, y) \rightarrow m(x, y) \wedge n(x, it), \\ m_2(x, y) \rightarrow m(x, y) \wedge n(x, dk) \}$$

GaV mapping $M_L =$

$$\{ m(x, y) \leftarrow m_1(x, y), \\ m(x, y) \leftarrow m_2(x, y), \\ n(x, y) \leftarrow m_1(x, z) \wedge y=it, \\ n(x, y) \leftarrow m_2(x, z) \wedge y=dk \}$$

Application to data integration

- $\text{After}^M(\varphi)$ is a **weakest precondition**
M is a GaV mapping
- $\text{Simp}^O_{\Delta}(\varphi) = \text{Weaken}_{\Delta}(\text{After}^O(\varphi))$

A condition about the global DB that can be checked on the local DBs

Conditions known to hold locally

Conditions to check globally

Example 1

$$\varphi = \leftarrow m(x, y) \wedge m(x, z) \wedge y \neq z$$

$$\varphi_1 = \leftarrow m_1(x, y) \wedge m_1(x, z) \wedge y \neq z$$

$$\varphi_2 = \leftarrow m_2(x, y) \wedge m_2(x, z) \wedge y \neq z$$

Check:

$$\left\{ \begin{array}{l} \leftarrow m_1(x, y) \wedge m_1(x, z) \wedge y \neq z, \\ \leftarrow m_1(x, y) \wedge m_2(x, z) \wedge y \neq z, \\ \leftarrow m_2(x, y) \wedge m_1(x, z) \wedge y \neq z, \\ \leftarrow m_2(x, y) \wedge m_2(x, z) \wedge y \neq z \end{array} \right\}$$

...

Example 1

$$\varphi = \leftarrow m(x, y) \wedge m(x, z) \wedge y \neq z$$

$$\varphi_1 = \leftarrow m_1(x, y) \wedge m_1(x, z) \wedge y \neq z$$

$$\varphi_2 = \leftarrow m_2(x, y) \wedge m_2(x, z) \wedge y \neq z$$

Check:

$$\{ \begin{array}{l} \leftarrow m_1(x, y) \wedge m_1(x, z) \wedge y \neq z, \\ \leftarrow m_1(x, y) \wedge m_2(x, z) \wedge y \neq z, \\ \leftarrow m_2(x, y) \wedge m_1(x, z) \wedge y \neq z, \\ \leftarrow m_2(x, y) \wedge m_2(x, z) \wedge y \neq z \end{array} \}$$

$$= \text{Simp}^M_{\varphi_1 \wedge \varphi_2}(\varphi)$$

...

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$$\varphi = \leftarrow m(x, y) \wedge m(x, z) \wedge y \neq z$$

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Check:

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$$= \text{Simp}^M_{\varphi_1 \wedge \varphi_2 \wedge \varphi_{1,2}}(\varphi)$$

$$\text{If we knew } \varphi_{1,2} = \leftarrow m_1(x, y) \wedge m_2(x, z)$$

Example 2

$$M = \{ f(i, t, r) \leftarrow m(i, t, y) \wedge r(i, r) \}$$

$$\varphi_1 = \{ \leftarrow m(i, t_1, y_1) \wedge m(i, t_2, y_2) \wedge t_1 \neq t_2, \\ \leftarrow m(i, t_1, y_1) \wedge m(i, t_2, y_2) \wedge y_1 \neq y_2 \}$$

$$\varphi_{1,2} = \leftarrow r(i, r) \wedge \neg m(i, t, y)$$

$$\varphi = \{ \leftarrow f(i, t_1, r_1) \wedge f(i, t_2, r_2) \wedge t_1 \neq t_2, \\ \leftarrow f(i, t_1, r_1) \wedge f(i, t_2, r_2) \wedge r_1 \neq r_2 \}$$

Global check:

$$\{ \leftarrow m(i, t_1, y_1) \wedge r(i, r_1) \wedge m(i, t_2, y_2) \wedge r(i, r_2) \wedge t_1 \neq t_2, \\ \leftarrow m(i, t_1, y_1) \wedge r(i, r_1) \wedge m(i, t_2, y_2) \wedge r(i, r_2) \wedge r_1 \neq r_2 \}$$

...

Example 2

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$$\varphi_{1,2} = \leftarrow r(i, r) \wedge \neg m(i, t, y)$$

$$\varphi = \{ \leftarrow f(i, t_1, r_1) \wedge f(i, t_2, r_2) \wedge t_1 \neq t_2, \\ \leftarrow f(i, t_1, r_1) \wedge f(i, t_2, r_2) \wedge r_1 \neq r_2 \}$$

Global check:

$$\{ \cancel{\leftarrow m(i, t_1, y_1) \wedge r(i, r_1) \wedge m(i, t_2, y_2) \wedge r(i, r_2) \wedge t_1 \neq t_2}, \\ \cancel{\leftarrow m(i, t_1, y_1) \wedge r(i, r_1) \wedge m(i, t_2, y_2) \wedge r(i, r_2) \wedge r_1 \neq r_2} \}$$

$$= \text{Simp}_{\varphi_1 \wedge \varphi_{1,2}}^M(\varphi)$$

Summary

- Express the data integration in terms of a GaV-mapping
- Reformulate the condition to check in terms of the sources by calculating a weakest precondition wrt the mapping
- Remove from it all conditions known to hold locally (plus possible cross-conditions)

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