DepQBF: A Dependency-Aware QBF Solver
(System Description)

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Edinburgh, Scotland, United Kingdom
## QBFsolver'10: Overall Score-Based Ranking

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This Talk:
- DepQBF 0.1 system overview.
- Selected features: restarts, removal of learnt constraints.
- Experimental evaluation.

http://www.qbflib.org/index_eval.php
DepQBF:
- Input: QBFs in Prenex-CNF (PCNF).
- QDPLL with conflict-driven clause and solution-driven cube learning.
- Analysis of variable dependencies.

Variable Dependencies in QBFs:
- PCNF $Q_1 Q_2 \ldots Q_n. \phi$: linearly ordered sets of quantified variables.
- Left-to-right prefix order: strong dependencies.
- DepQBF: relaxing prefix order by dependency schemes.

Example

Quantifier ordering matters:
- $\forall x \exists y. (x = y)$ is satisfiable: value of $y$ depends on value of $x$.
- $\exists y \forall x. (x = y)$ is unsatisfiable: value of $y$ is fixed for all values of $x$. 
Dependency Schemes: \( D \subseteq (V_\exists \times V_\forall) \cup (V_\forall \times V_\exists) \). [SS09, LB09, LB10, Ben05]

- \((x, y) \notin D\): \(y\) independent from \(x\).
- \((x, y) \in D\): conservatively regard \(y\) as depending on \(x\).

**DepQBF:** *standard dependency scheme* \( D^{\text{std}} \subseteq D^{\text{triv}} \).

- Previous work: \( D^{\text{std}} \) as dependency-DAG over equivalence classes.
- Efficient integration.

**Example:** \( \exists a, b \forall x, y \exists c, d. (a \lor x \lor c) \land (a \lor b) \land (b \lor d) \land (y \lor d) \).

\[
\begin{align*}
\exists a & \quad \exists b \\
\forall x & \quad \forall y \\
\exists c & \quad \exists d
\end{align*}
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\begin{align*}
\exists a & \quad \exists b \\
\forall x & \quad \forall y \\
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\]

\( D^{\text{std}} \) \quad \( D^{\text{triv}} \)

Standard dependency scheme \( D^{\text{std}} \), quantifier prefix \( D^{\text{triv}} \).
Figure: DepQBF workflow.

Boolean Constraint Propagation (BCP):

- Propagation of unit and pure literals.
- Watched data-structures for efficient detection.
Initialize Dependency-DAG:

- Top-most decision level 0.
- All assignments at top-level are permanent.
- Permanent simplifications (satisfied clauses).
- Potential reduction of dependencies.
Retrieval Decision Candidates (DC):

- Get possible decision variables (candidates) from dependency-DAG.
- Candidate: all “preconditions” (predecessors in DAG) assigned.
- Candidate set is maintained incrementally and lazily.

Figure: DepQBF workflow.
System Overview (4/7)

Decision Making:
- Select decision variable from candidate set.
- Activity-based priority queue of variables (VSIDS, like MiniSAT 2).
- Assignment caching.

Figure: DepQBF workflow.
Figure: DepQBF workflow.

Constraint Learning (Result Analysis):

- Conflict/solution: generate *asserting* learnt clause/cube.
- Augmented CNF: $\phi := \phi_{OCL} \land (\phi_{LCL} \lor \phi_{LCU})$.
- Learnt clauses $\phi_{LCL}$ and cubes $\phi_{LCU}$.
- Q-resolution/consensus to derive learnt clauses/cubes.
- See also our SAT’10 paper.
Figure: DepQBF workflow.

Learnt Constraint Removal and Restarts:
- Check each time when adding a new learnt constraint.
- Capacity exhausted: remove half of learnt constraints.
- Heuristically try to keep “useful” constraints, increase capacity.
- Inner-outer restart schedule (like PicoSAT).
Backtracking:

- General (frequent) case: backtrack to asserting level of learnt constraint.
- Special case: backtrack to restart level.
Learnt Constraint Removal

**Learnt Constraints:** [GNT02, Let02, ZM02, GNT06, BKF95, GS08, ES03, GN02]
- Clauses $\phi_{LCL}$ and cubes $\phi_{LCU}$, stored in doubly-linked lists.
- Initial capacities depend on formula size: [2500, 10000].

**Move-To-Front (MTF) Strategy:** approximating clause activities.
- Want to keep “used” (i.e. important?) constraints: units, learning.
- Move used constraints $C_i$ to head of list:

\[
\{ C_1, \ldots, C_{i-1}, C_i, C_{i+1}, \ldots, C_n \} \xrightarrow{MTF(C_i)} \{ C_i, C_1, \ldots, C_{i-1}, C_{i+1}, \ldots, C_n \}
\]

most-recently used \hspace{1cm} least-recently used \hspace{1cm} deletion order

**Deletion:**
- Capacity exhausted: remove half of constraints, starting at tail of list.
- Least-recently used ones are deleted (hopefully: least-important ones).
- Increase capacity by constant 500.
**Inner-Outer Restart Schedule:** when to restart?  

- Inspired by PicoSAT: separate inner/outer restarts.  
- Inner restart after $i$ backtracks, outer restart after $o$ inner restarts.  
- Initially $i := 100$, $o := 10$.  
- Before $i$th ordinary backtrack: jump to *restart level* instead, $i := i + 10$.  
- After $o$ inner restarts: $i := 100$, $o := o + 5$ (outer restart).

![Graph showing inner distance versus restarts](image-url)
**Restart Level:** where to jump to?

- Normally, DepQBF always jumps to asserting level.
- Restart: possibly jump *most-recent universal decision level* instead.
  - Always the longer jump is taken.
- Related to ideas from unrestricted backtracking [BLdSMS05].

**Example:**

- Assignment stack, in order of decision levels.
- Conflict/solution at level 4.
- Restart is scheduled, where to jump to?
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- Restart: possibly jump *most-recent universal decision level* instead.
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- Related to ideas from unrestricted backtracking [BLdSMS05].

**Example:**
- Current learnt constraint asserting at level 3.
- Last universal decision at level 2.
**Restart Level:** where to jump to?

- Normally, DepQBF always jumps to asserting level.
- Restart: possibly jump *most-recent universal decision level* instead.
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- Related to ideas from unrestricted backtracking [BLdSMS05].

**Example:**

- Current learnt constraint asserting at level 3.
- Last universal decision at level 2.
- **Restart:** take the longer jump.
**Restart Level:** where to jump to?

- Normally, DepQBF always jumps to asserting level.
- Restart: possibly jump *most-recent universal decision level* instead.
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- Related to ideas from unrestricted backtracking [BLdSMS05].

**Example:**

- Current learnt constraint asserting at level 1.
- Last universal decision at level 2.
**Restart Level:** where to jump to?
- Normally, DepQBF always jumps to asserting level.
- Restart: possibly jump *most-recent universal decision level* instead.
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- Related to ideas from unrestricted backtracking [BLdSMS05].

**Example:**
- Current learnt constraint asserting at level 1.
- Last universal decision at level 2.
- **Restart:** take the longer jump.
### Experiments: QBFEVAL’10 Main Track

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**Table:** QBFEVAL’10 main track (568 formulae). Ranking by number of solved formulae.

**Setup:**
- Ubuntu 9.04, Intel® Q9550@2.83 GHz, 3 GB/900 sec.
- DepQBF: version 0.1 which participated in QBFEVAL’10.
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**Important:**
- Restarts (disabled in DepQBF-nr).
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**Important:**
- **Restarts.**
- **Assignment caching** (disabled in DepQBF-nc).
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### Important:
- Re却ts.
- Assignment caching.
- Pure literal detection (disabled in DepQBF-np).
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**Important:**
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- Pure literal detection.
- Combining restarts with assignment caching (disabled in DepQBF-ncnr).
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Important:
- Restarts.
- Assignment caching.
- Pure literal detection.
- Combining restarts with assignment caching.
- Preprocessing (not part of DepQBF 0.1, disabled in QuBE*-nopp).
Experiments: QBFEVAL’10 Main Track

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DepQBF: A Dependency-Aware QBF Solver (System Description)
DepQBF:

- Search-based QBF solver with clause- and cube-learning.
- Relaxing prefix order by dependency-DAG for $D^{\text{std}}$.
- Approaches from SAT domain.
- Development:
  - Fuzz testing using QBFuzz: [http://fmv.jku.at/qbfuzz/](http://fmv.jku.at/qbfuzz/)
  - Delta-debugging using QBFDD: [http://fmv.jku.at/qbfdd/](http://fmv.jku.at/qbfdd/)
  - Cross-checking against other solvers, mainly QuBE.

Performance:

- Top-ranked solver in QBFEVAL’10.
- DepQBF 0.1 does not include preprocessing.
- But: preprocessing is very important.

Future Work:

- Preprocessing, parameter tuning, decision heuristics, ...

DepQBF 0.1 is open source: [http://fmv.jku.at/depqbf/](http://fmv.jku.at/depqbf/)
Unit Clauses: Clause $C$ is unit iff 

- no $l \in C$ is true.
- exactly one $l_e \in L_\exists(C)$ is unassigned.
- for all unassigned $l_u \in L_\forall(C)$: $l_u \not\preceq l_e$, i.e. $\text{Var}(l_u), \text{Var}(l_e)$ independent.
- Dependency checking $\prec$ with respect to dependency scheme.
- Dual definition for cubes.

Two-Literal-Watching:

- Watch two unassigned literals $l_1, l_2 \in C$ such that 
  1. either $q(l_1) = q(l_2) = \exists$, or 
  2. $q(l_1) = \forall$, $q(l_2) = \exists$ and $l_1 \prec l_2$.

Watcher Update:

- Dependency checking needed only in case (2).
- Stop when finding satisfying literal.
- No work needed during backtracking.
Pure Literals (PL):
- Variable has only positive/negative literals left.
- Assigning $\forall$-PLs/$\exists$-PLs can trigger new units/further PLs.
- Drawback: expensive detection in $\phi_{OCL} \land (\phi_{LCL} \lor \phi_{LCU})$.

Spurious Pure Literals (SPL):
- Def.: Variable is pure (SPL) if it is pure in original clauses $\phi_{OCL}$ only.
- SPL-Detection neglects all learnt constraints in $(\phi_{LCL} \lor \phi_{LCU})$.
  - Advantage: more efficient detection.
- Variable might be pure in $\phi_{OCL}$ but not in $\phi_{OCL} \land (\phi_{LCL} \lor \phi_{LCU})$.
  - Drawback: must ignore such SPL-implications in $(\phi_{LCL} \lor \phi_{LCU})$.

Clause Watching:
- Positive/negative occurrences $C(x), C(\overline{x}) \subseteq \phi_{OCL}$.
- Watch two unsatisfied clauses $C_x \in C(x)$ and $C_{\overline{x}} \in C(\overline{x})$. 

[CGS98, GGN$^+$03, GNT04]
Clause Watcher Update:
- Assign $x/\overline{x}$: all clauses in $C(x)/C(\overline{x})$ will be satisfied.
- Update watchers of variables $y$ watching clauses in $C(x)/C(\overline{x})$.

Notification Lists:
- Goal: avoid searching for variables which need watcher update.
- Lists $NL_x/NL_{\overline{x}}$ of variables $y$ watching clauses in $C(x)/C(\overline{x})$.
- Assign $x/\overline{x}$:
  - *exactly* all variables in $NL_x/NL_{\overline{x}}$ must update their watcher.
  - update $NL_x/NL_{\overline{x}}$ of variables $x$ occurring in old and new watched clauses.
- No work needed during backtracking.
Activity-Based Variable Priority Queue:  

- DepQBF: straight-forward generalization of idea from SAT domain.
- Maintain VSIDS score (activity) for each variable.
- Increase activity of variables encountered during learning.
- Periodically down-scale activities.
- Implementation follows MiniSAT 2.
- Decision making: select *candidate* with highest activity.
- Lazy priority queue maintenance (like in MiniSAT):
  - Discard assigned variables and non-candidates on the fly upon removal.
Also called: Phase Saving

- DepQBF: straight-forward generalization of idea from SAT-domain.
- Each variable has a cached assignment (possibly undefined).
- All assignments (unit, pure literals, decisions) update cache.
- Decision variables: assign cached value, if any.
- No distinction between different quantifiers.
## Suite mqm (136 formulae)

<table>
<thead>
<tr>
<th>Solver</th>
<th>solved</th>
<th>avg.time</th>
</tr>
</thead>
<tbody>
<tr>
<td>DepQBF</td>
<td>136</td>
<td>39.83</td>
</tr>
<tr>
<td>QuBE7</td>
<td>117</td>
<td>306.43</td>
</tr>
<tr>
<td>QuBE7.0-nopp</td>
<td>115</td>
<td>304.82</td>
</tr>
<tr>
<td>QuBE6.6</td>
<td>100</td>
<td>393.93</td>
</tr>
<tr>
<td>QuBE6.6-nopp</td>
<td>97</td>
<td>399.55</td>
</tr>
</tbody>
</table>

**Table**: Solvers sorted by number of solved formulae.

**Benchmark Suite *mqm***:
- Minimal Query Inseparability Module Extraction in DL-Lite.
- Newly submitted to QBFEVAL’10 by Roman Kontchakov.
- As the only solver, DepQBF solved entire suite in QBFEVAL’10.
### QBFEVAL’10: solved formulae only

<table>
<thead>
<tr>
<th></th>
<th>∩</th>
<th>SAT-∩</th>
<th>UNSAT-∩</th>
</tr>
</thead>
<tbody>
<tr>
<td>solved</td>
<td>328</td>
<td>132</td>
<td>196</td>
</tr>
<tr>
<td>avg.time</td>
<td>84.97</td>
<td>21.87</td>
<td>140.16</td>
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</tbody>
</table>

### QBFEVAL’10: unique results

<table>
<thead>
<tr>
<th></th>
<th>SAT-⇔</th>
<th>UNSAT-⇔</th>
</tr>
</thead>
<tbody>
<tr>
<td>solved</td>
<td>86</td>
<td>42</td>
</tr>
</tbody>
</table>

Table: QuBE7 (left columns) vs. DepQBF (right columns).

### QBFEVAL’10: solved formulae only

<table>
<thead>
<tr>
<th></th>
<th>∩</th>
<th>SAT-∩</th>
<th>UNSAT-∩</th>
</tr>
</thead>
<tbody>
<tr>
<td>solved</td>
<td>308</td>
<td>115</td>
<td>193</td>
</tr>
<tr>
<td>avg.time</td>
<td>80.14</td>
<td>17.49</td>
<td>114.17</td>
</tr>
</tbody>
</table>

### QBFEVAL’10: unique results

<table>
<thead>
<tr>
<th></th>
<th>SAT-⇔</th>
<th>UNSAT-⇔</th>
</tr>
</thead>
<tbody>
<tr>
<td>solved</td>
<td>79</td>
<td>62</td>
</tr>
</tbody>
</table>

Table: QuBE6.6 (left columns) vs. DepQBF (right columns).


N. Eén and N. Sörensson.
An Extensible SAT-Solver.

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R. Letz.
Lemma and Model Caching in Decision Procedures for Quantified
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