



Business Informatics Group

Vienna University of Technology



WIENER WISSENSCHAFTS-,
FORSCHUNGS- UND TECHNOLOGIEFONDS

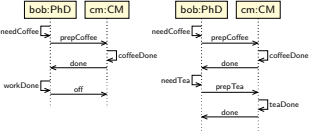
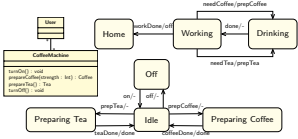
Guided Merging of Sequence Diagrams



Magdalena Widl

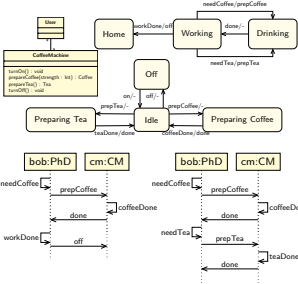
Knowledge-Based Systems Group
Vienna University of Technology

Motivation and Scope



Motivation and Scope

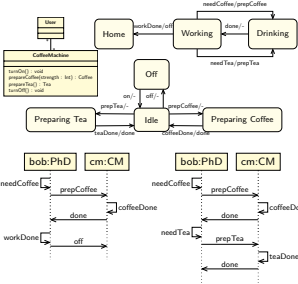
Model-Driven Engineering



Motivation and Scope

Model-Driven Engineering

Model Evolution

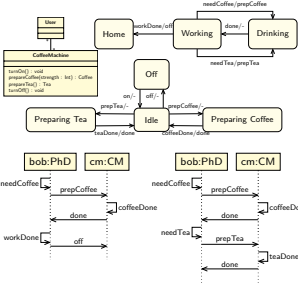


Motivation and Scope

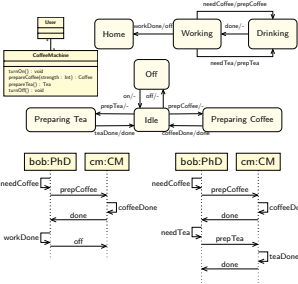
Model-Driven Engineering

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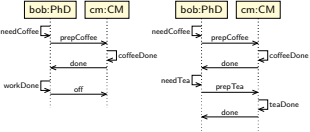


Model-Driven Engineering

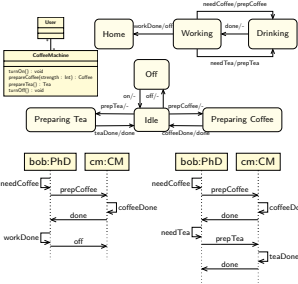
Model Evolution

Model Versioning

Model Merging



Motivation and Scope



Model-Driven Engineering

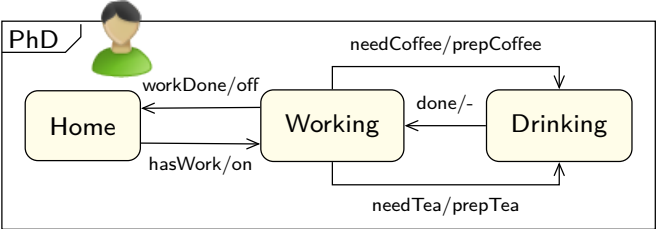
Model Evolution

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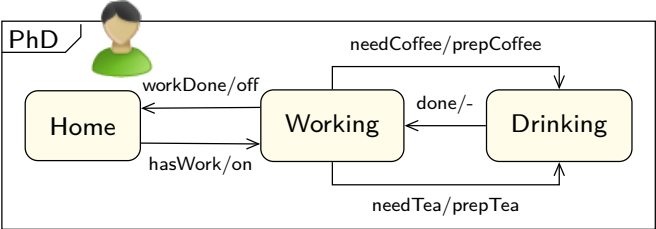
Model Merging

Multi-View Modelling

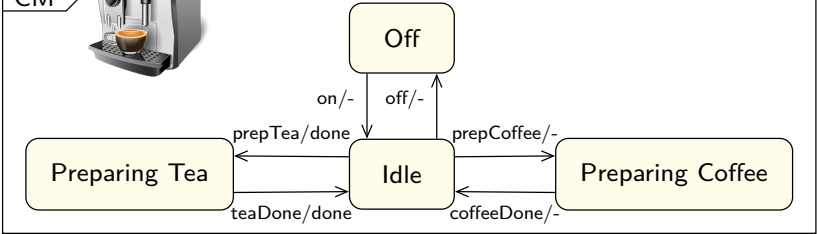
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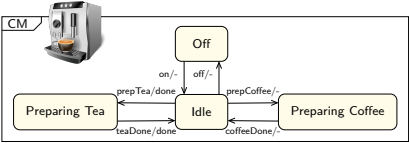
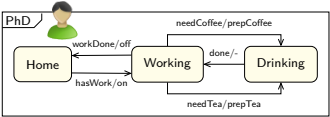
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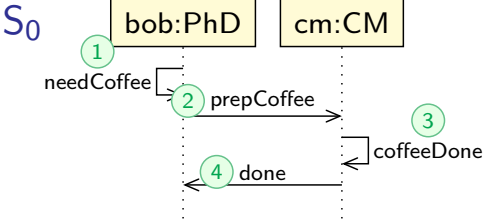
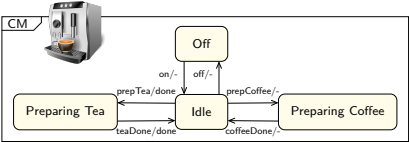
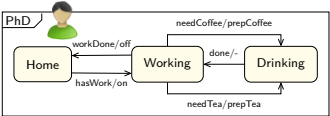
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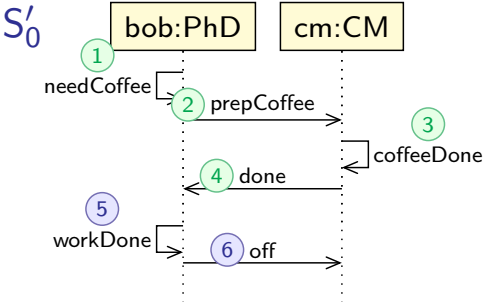
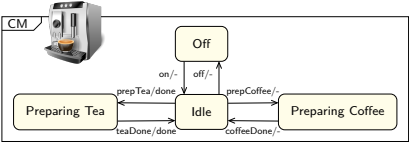
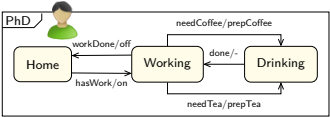
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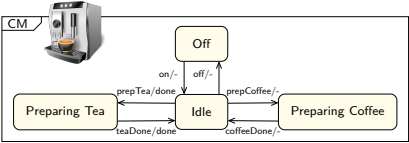
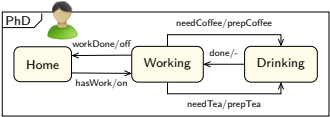
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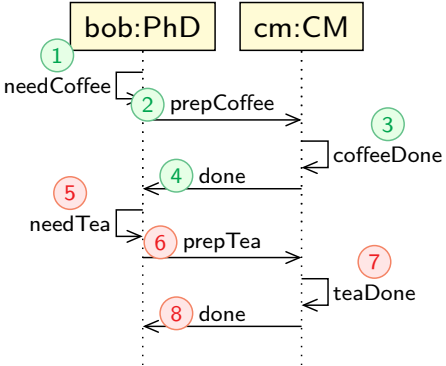
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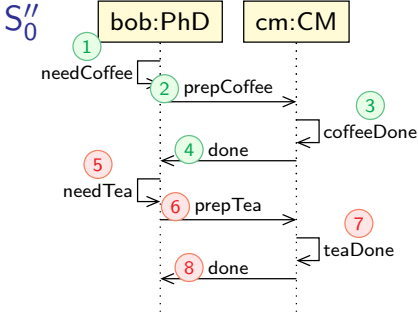
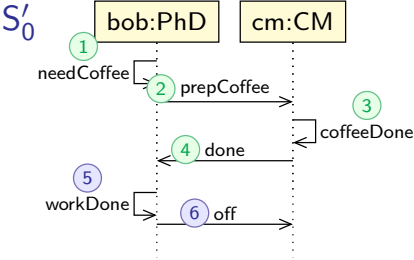
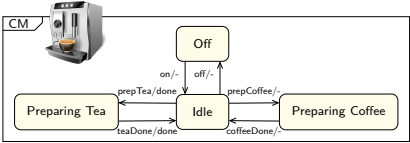
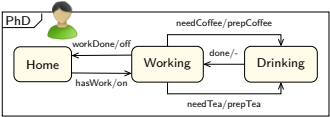
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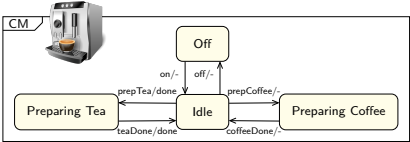
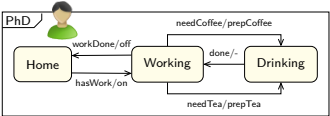
S''_0



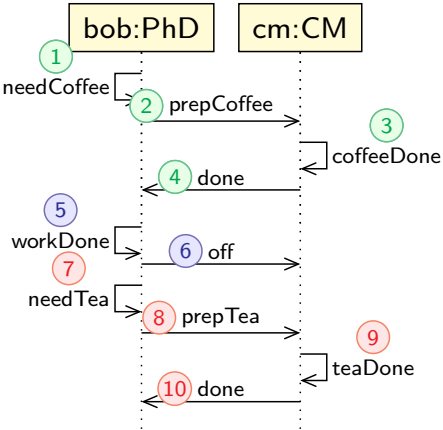
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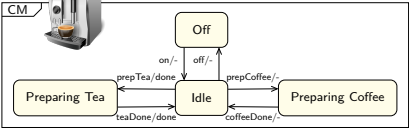
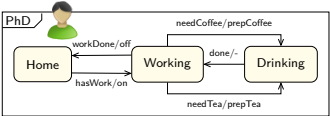
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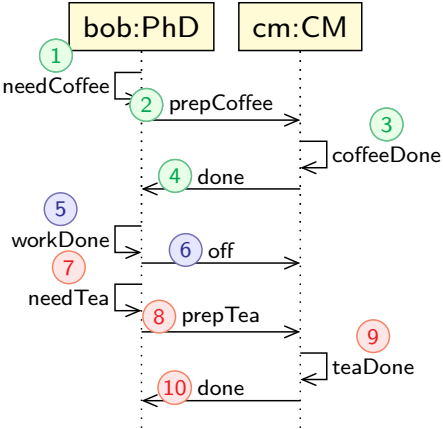
$S_1 ?$



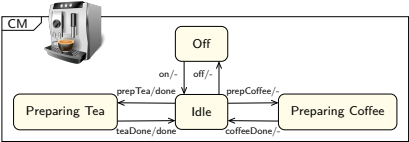
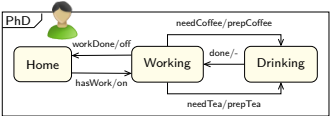
Example



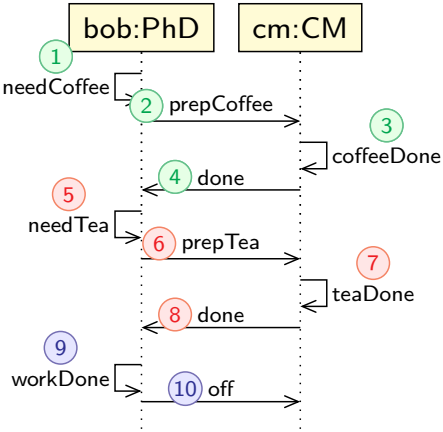
S_1 ?



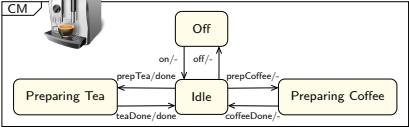
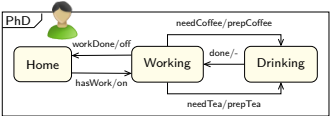
Example



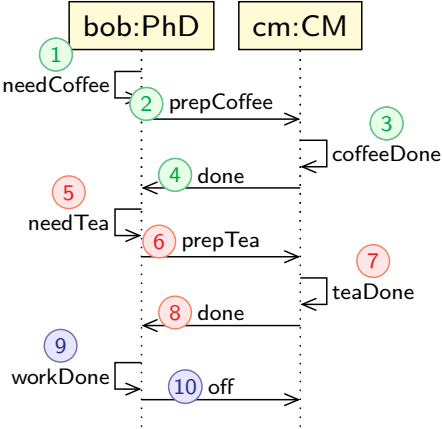
S_1 ?



Example



S_1 ?



Guided Merging of Sequence Diagrams

Why? No more cumbersome manual merging!



Guided Merging of Sequence Diagrams

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Challenges

- Model merging is much more complex than text merging



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- Implementation and evaluation



Guided Merging of Sequence Diagrams

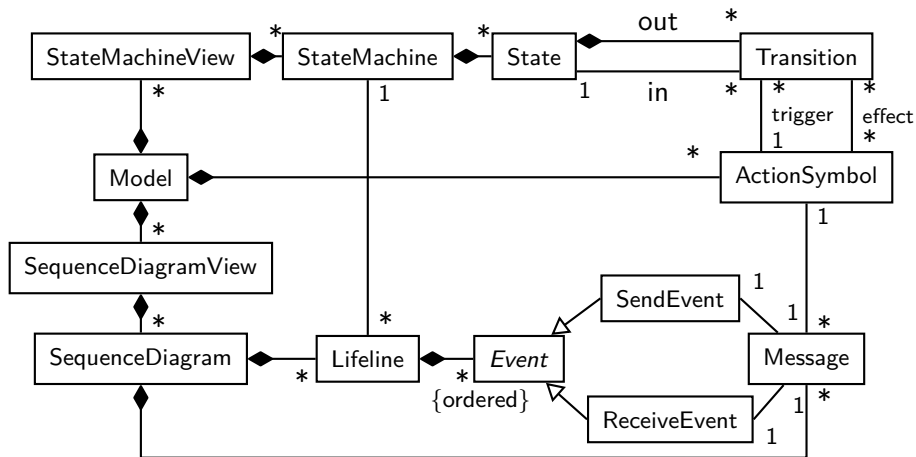
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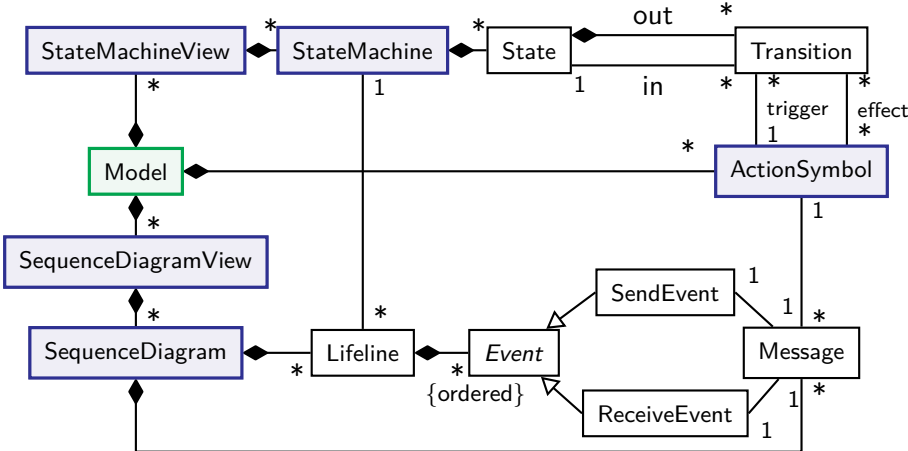
Formalization

The *tMVML* Metamodel



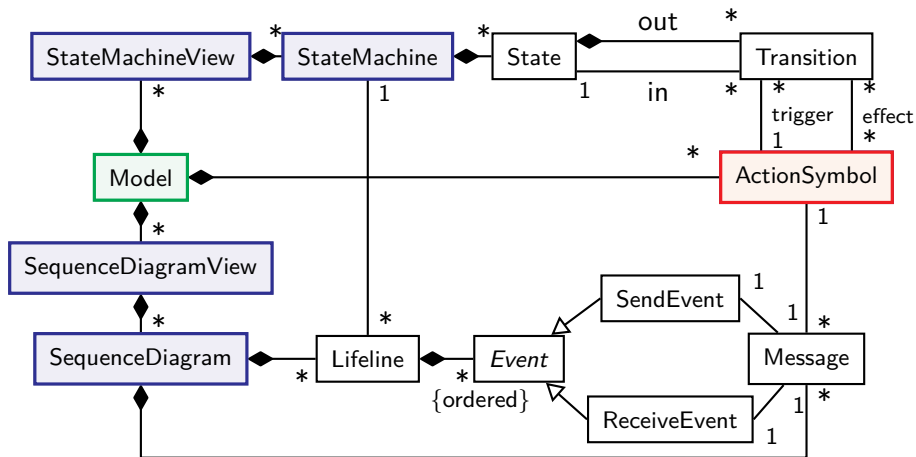
Formalization

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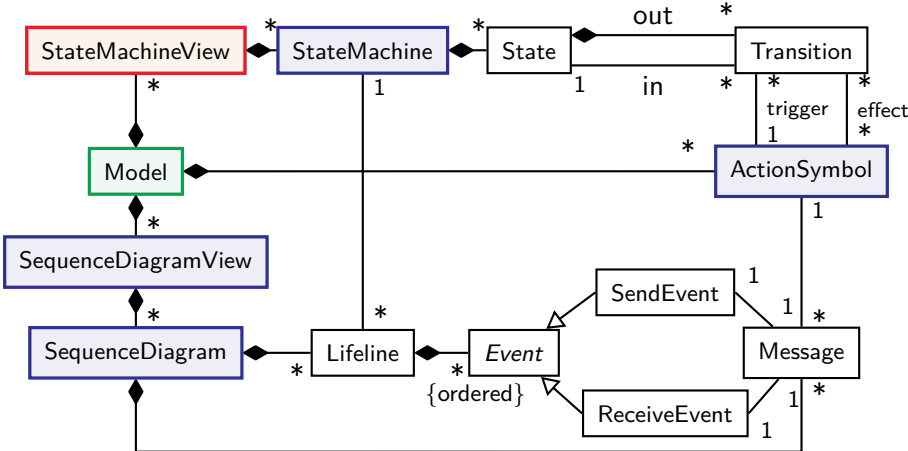
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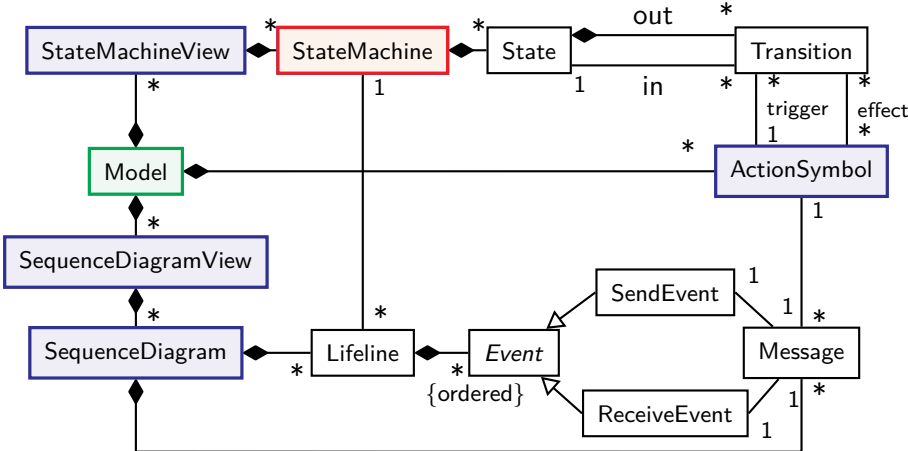
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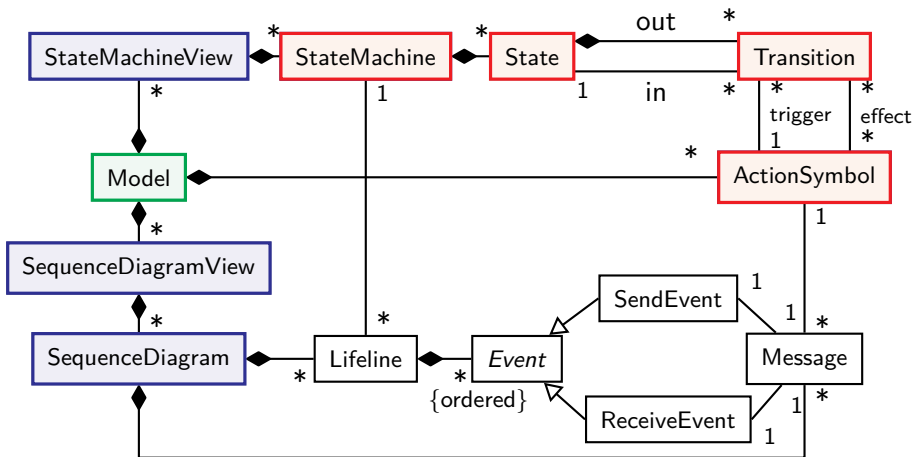
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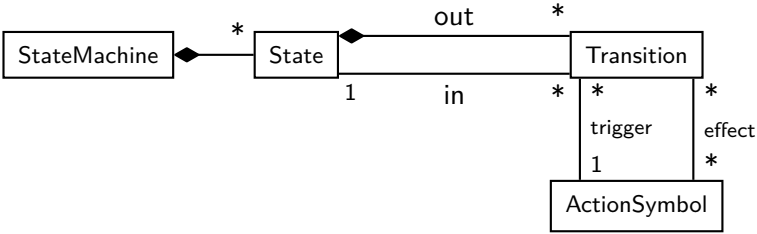
Formalization

The *t*MVML Metamodel



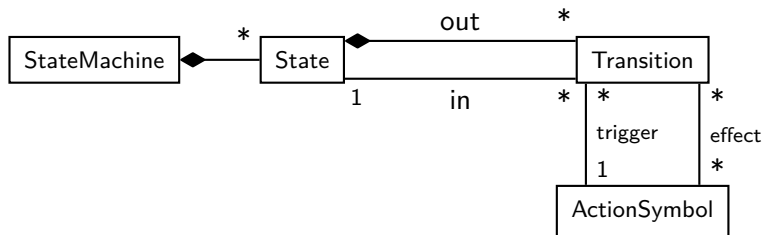
Formalization

State Machine



Formalization

State Machine



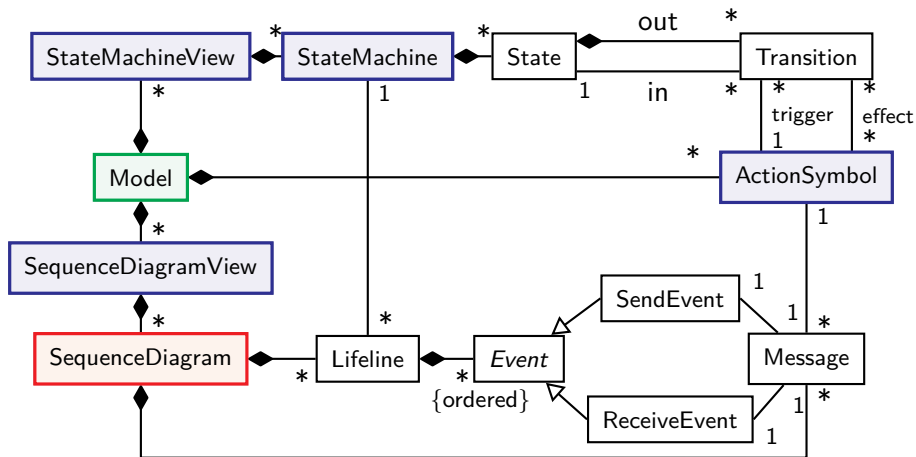
Given an alphabet \mathcal{A}_A , a state machine is a quadruple (S, A^{tr}, A^{eff}, T) , where

- S is a set of states,
- $A^{tr}, A^{eff} \subseteq \mathcal{A}_A$ are sets of action symbols, and
- $T \subseteq (S \times A^{tr} \times \mathcal{P}(A^{eff}) \times S)$ is a relation representing the transitions between states.



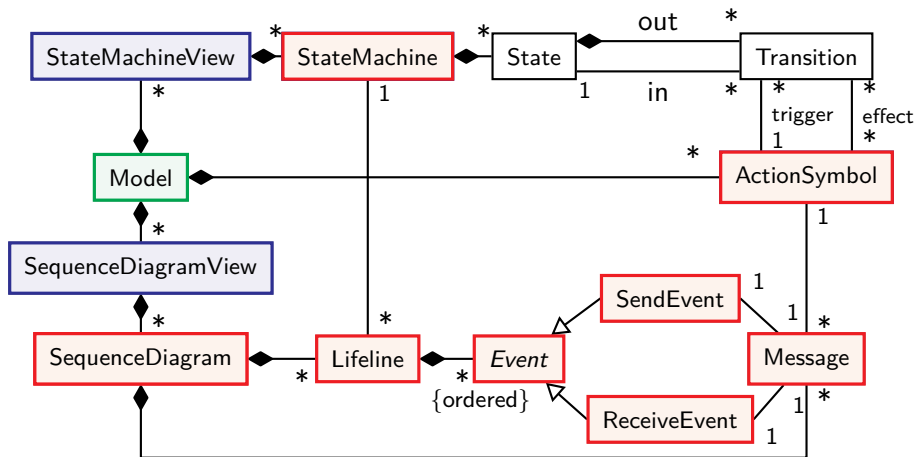
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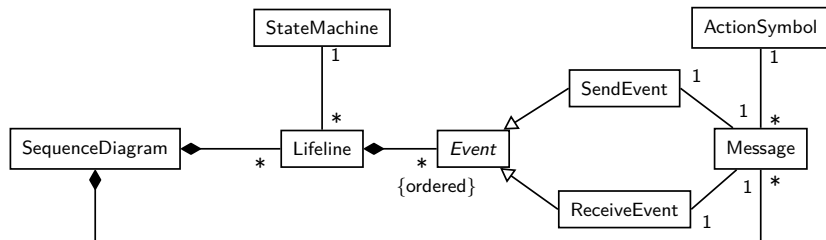
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The *t*MVML Metamodel



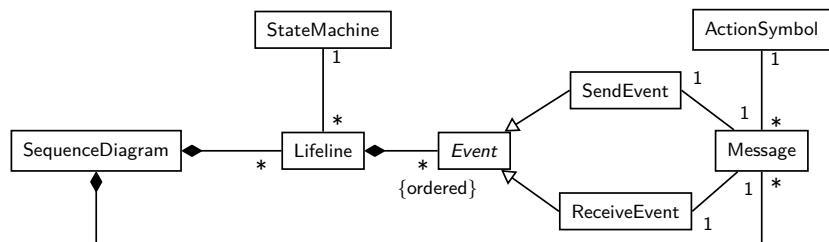
Formalization

Sequence Diagram



Formalization

Sequence Diagram



Given the alphabets \mathcal{A}_A and \mathcal{A}_E , and a set \mathcal{SM} of state machines, a sequence diagram is a quadruple $(L, M, \text{life}, \text{msg})$, where

- L is a set of lifelines,
- M is a set of messages,
- $\text{life} : L \rightarrow (\mathcal{SM} \times \mathcal{P}(\mathcal{A}_E) \times \mathcal{P}(\mathcal{A}_E) \times \mathcal{P}(\mathcal{A}_E \times \mathcal{A}_E))$
- $\text{msg} : M \rightarrow (\mathcal{A}_A \times \bigcup_{l \in L} \pi_2(\text{life}(l)) \times \bigcup_{l \in L} \pi_3(\text{life}(l)))$.



Formalization

Sequence Diagram

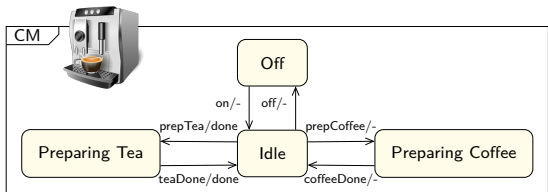
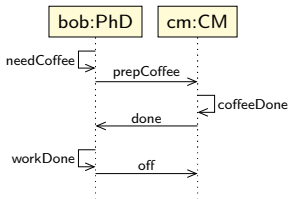
Lifeline conformance: For each lifeline, the sequence of received message symbols is a path of triggers in the attached state machine.



Formalization

Sequence Diagram

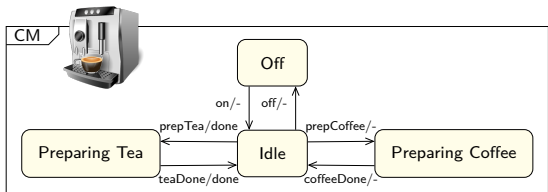
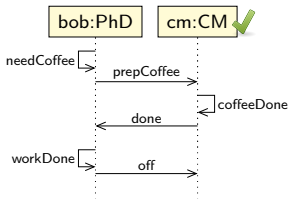
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Formalization

Sequence Diagram

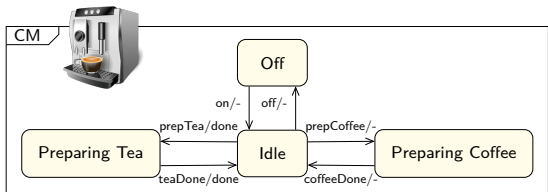
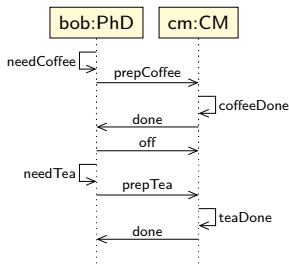
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Formalization

Sequence Diagram

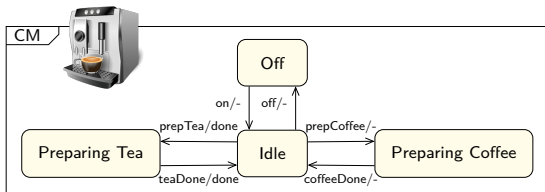
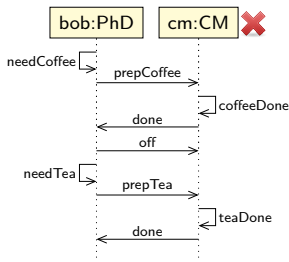
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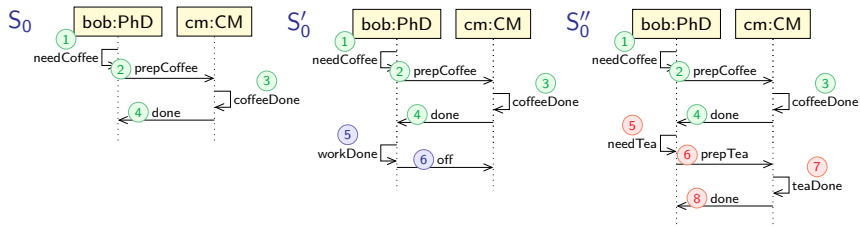
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Problem statement

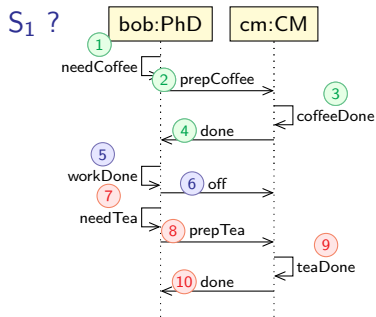
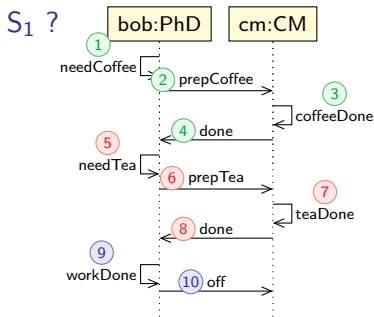
Instance: A sequence diagram and two of its *revisions*.



Problem statement

Objective: Find a *consolidated version*

- Contains all original and added messages and lifelines
- Lifelines conform to state machines



Our Contributions

- Formalization of state machine, sequence diagram, formal problem statement
- **Translation to propositional SAT Problem**
- Implementation and evaluation



Translation to propositional SAT

Three types of variables

- m_i , m : message, i : position
- c_i^s , s : state in state machine, i : position, c : “source”
- t_i^s , s : state in state machine, i : position, t : “target”



Translation to propositional SAT

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Propositional formula consists of constraints that describe legal solutions, e.g.

$$(m_1 \vee m_2 \vee m_3) \wedge (\neg m_1 \vee \neg m_2) \wedge (\neg m_2 \vee \neg m_3) \wedge (\neg m_1 \vee \neg m_3)$$



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$$m_1 \rightarrow ((c_1^{s1} \wedge t_1^{s2}) \vee (c_1^{s3} \wedge t_1^{s4}))$$



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$$m_1 \rightarrow ((c_1^{s1} \wedge t_1^{s2}) \vee (c_1^{s3} \wedge t_1^{s4}))$$

The encoding is polynomial in the input size.

Satisfying assignments of the formula can be directly translated back into a solution of our problem.



Translation to propositional SAT

$$\begin{aligned}
 & \bigwedge_{m \in M} \left(\bigvee_{i \in \text{allow}(m)} m_i \right) \wedge \bigwedge_{m \in M} \bigwedge_{\substack{i, j \in \text{allow}(m) \\ i \neq j}} \left(\neg m_i \vee \neg m_j \right) \\
 & \bigwedge_{x \in \{o, \alpha, \beta\}} \bigwedge_{m \in M^x} \bigwedge_{i \in \text{allow}(m)} \left(\neg m_i \vee \bigvee_{\substack{n \in M^x, \\ n \succ m}} \bigvee_{j \in \text{allow}(n)} n_j \right) \\
 & \bigwedge_{i \in \text{allow}(m)} \left(\neg m_i \vee \bigvee_{t \in \text{trans}(m)} (c_i^{\pi_1(t)} \wedge t_i^{\pi_4(t)}) \right) \\
 & \bigwedge_{i=1}^k \left(\left(\bigvee_{c_i^s \in \text{vc}} c_i^s \right) \wedge \left(\bigvee_{t_i^s \in \text{vt}} t_i^s \right) \wedge \bigwedge_{s \in S_{\text{all}}} \bigwedge_{r \in S_{\text{all}} \setminus s} \left((\neg c_i^s \vee \neg c_i^r) \wedge (\neg t_i^s \vee \neg t_i^r) \right) \right) \\
 & \bigwedge_{i=1}^{k-1} \bigwedge_{M \in \mathcal{SM}} \bigwedge_{s \in \pi_1(SM)} \\
 & \left(\left(t_i^s \rightarrow \bigwedge_{r \in \pi_1(SM) \setminus s} \neg c_{i+1}^r \right) \wedge \left(\bigwedge_{j=1}^i (t_i^s \wedge \bigwedge_{l=1}^j \neg c_l^s \rightarrow \bigwedge_{r \in \pi_1(SM) \setminus s} \neg c_{j+1}^r) \right) \right)
 \end{aligned}$$



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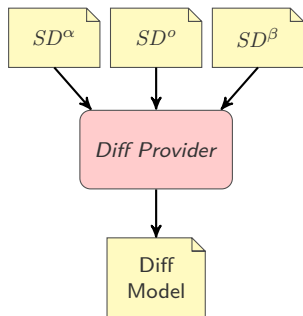
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- Translation to propositional SAT Problem
- **Implementation and evaluation**



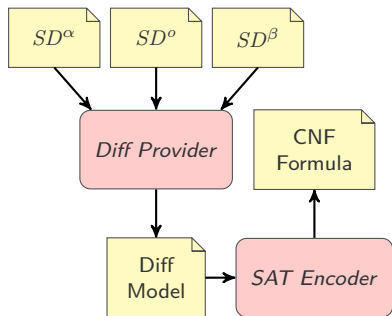
Implementation – Workflow



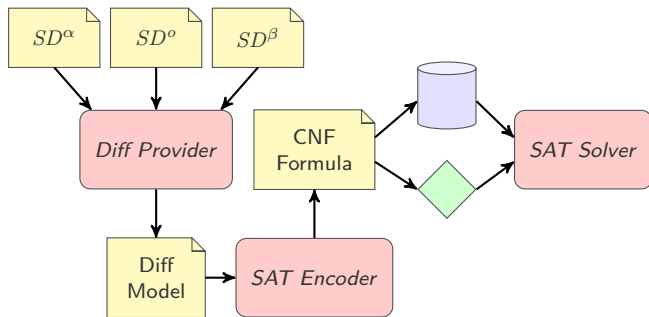
Implementation – Workflow



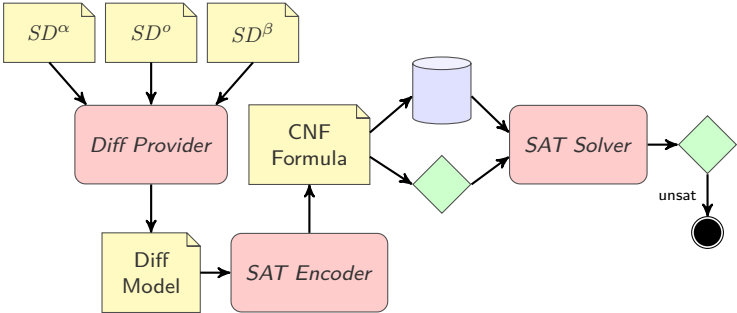
Implementation – Workflow



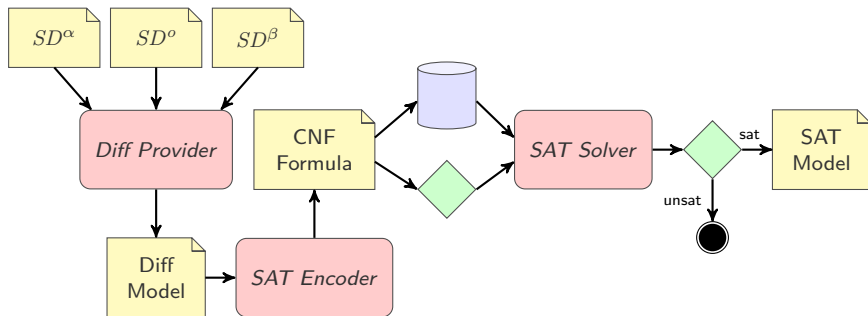
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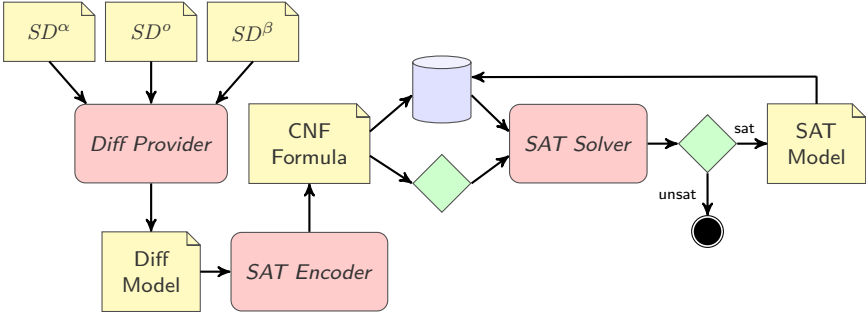
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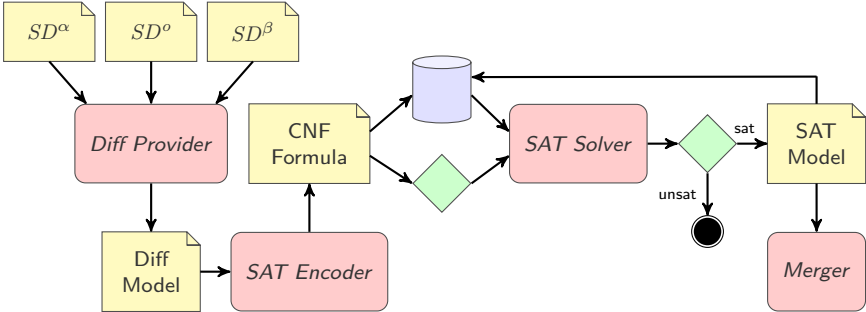
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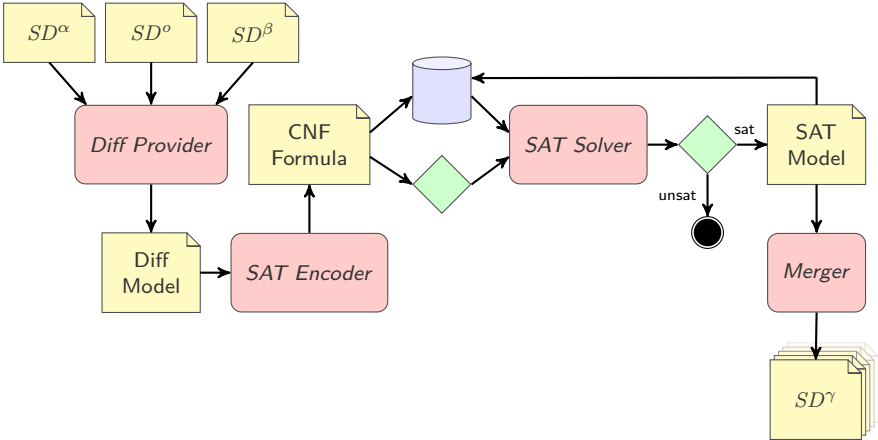
Implementation – Workflow



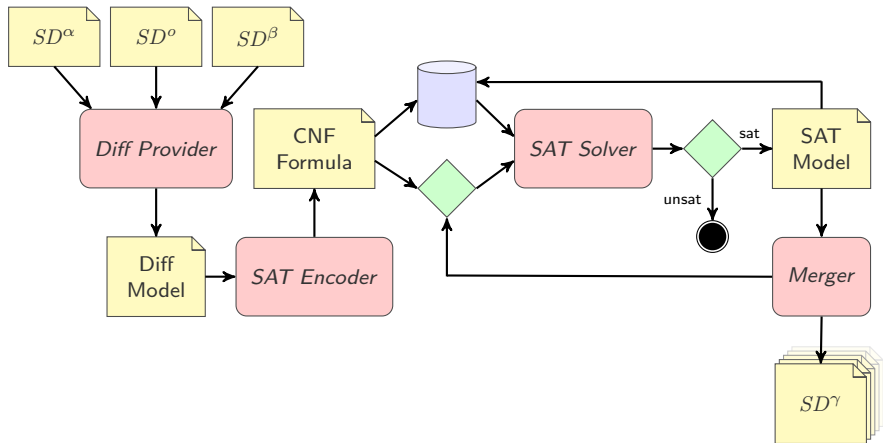
Implementation – Workflow



Implementation – Workflow



Implementation – Workflow



Evaluation

- Benchmark set with 45 instances



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- For some instances, no state machines are defined



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email	3	15	16	19
coffee	2	9	7	8
philosopher	2	8	7	8



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Results

- Between 0.06s and 0.2s per solution depending on instance



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Results

- Between 0.06s and 0.2s per solution depending on instance
- Some instances have many solutions (>1,000)



Summary and Future Work

We

- Formalized a subset of the UML in our language *tMVML*



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What we consider next

- Handling high numbers of solutions



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What we consider next

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- Integration of other UML concepts
- Visualization



Related Work

Model merging:

- *Gerth et al.*, Merge support for business process models using term rewriting systems
- *Cicchetti et al.*, Definition of conflict patterns
- *Nejati et al.*, Merging of state machines

Consistency checking:

- *Diskin et al.*, Category theory based framework
- *Van der Straeten et al.*, Inconsistency detection between class and sequence diagrams using Kodkod
- *Sabatzadeh et al.*, Consistency checks between overlapping models
- *Tsoliakis*, Integration of constraints of other views into sequence diagrams
- *Brosch et al.*, Model checking on state machines and sequence diagrams

