



WIENER WISSENSCHAFTS-
FORSCHUNGS- UND TECHNOLOGIEFONDS

Business Informatics Group

Vienna University of Technology

A SAT-based Debugging Tool for State Machines and Sequence Diagrams



Petra Kaufmann, Martin Kronegger,
Andreas Pfandler, Martina Seidl,
Magdalena Widl

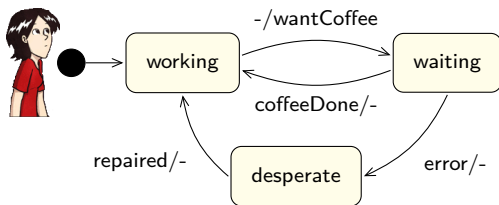
State Machines



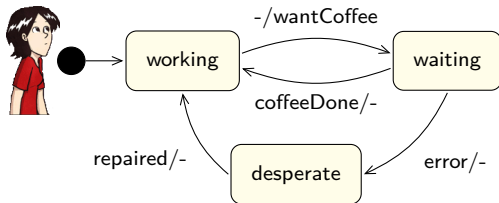
Image courtesy of "Piled Higher and Deeper" by Jorge Cham www.phdcomics.com



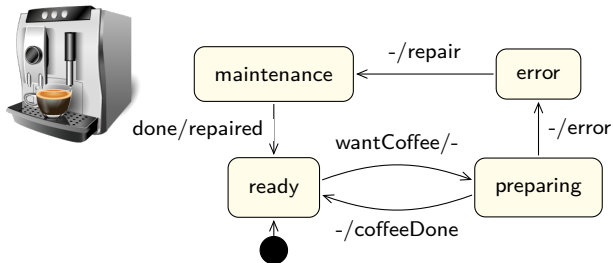
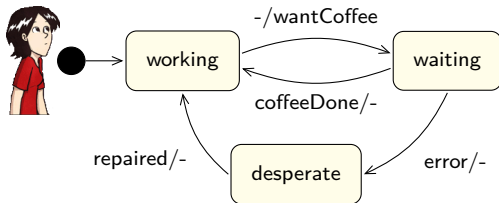
State Machines



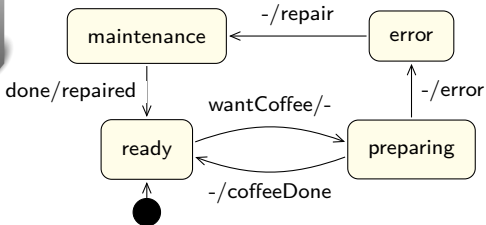
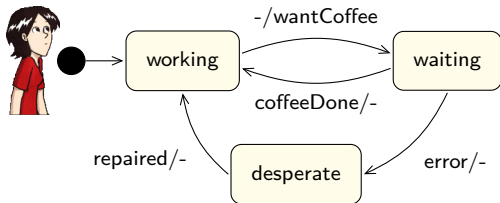
State Machines



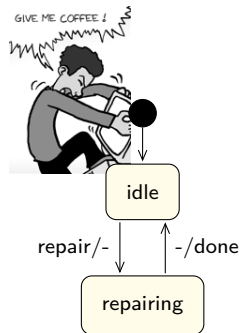
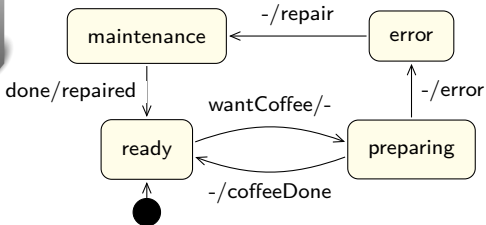
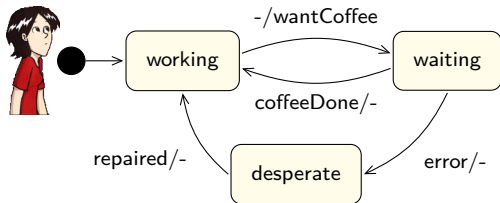
State Machines



State Machines



State Machines



State Machines

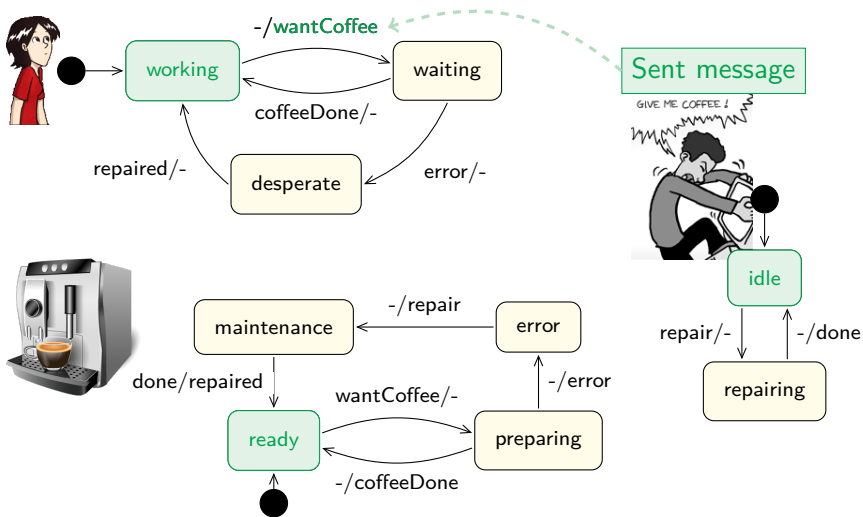
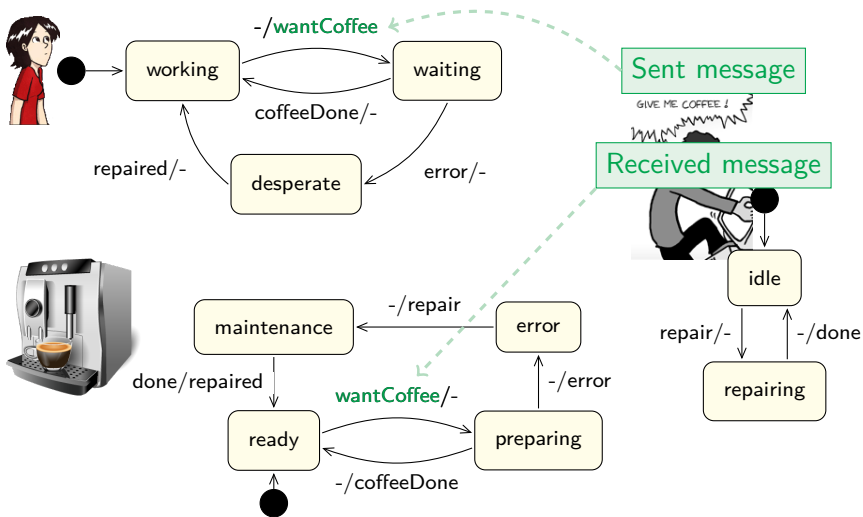


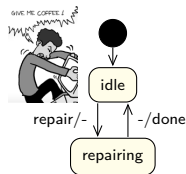
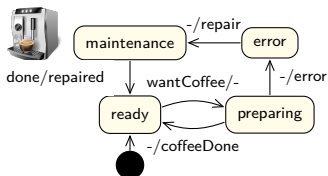
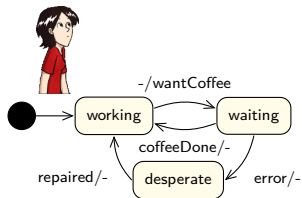
Image courtesy of "Piled Higher and Deeper" by Jorge Cham www.phdcomics.com



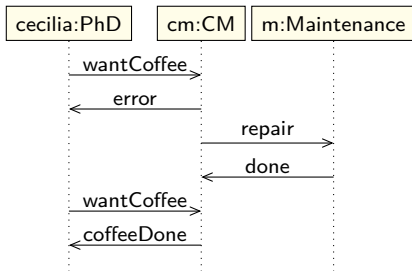
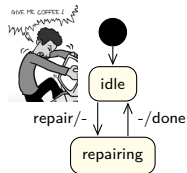
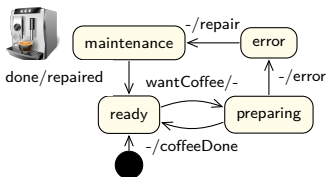
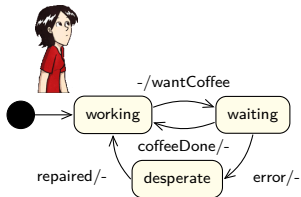
State Machines



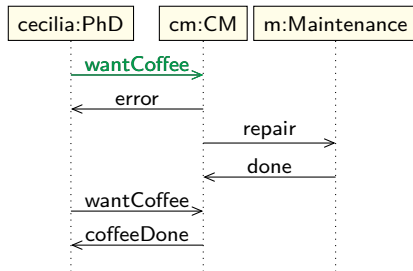
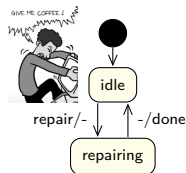
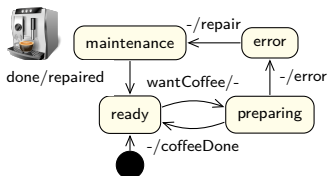
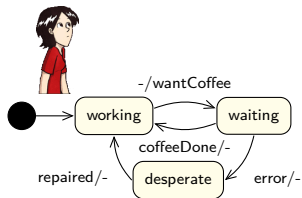
Sequence Diagram



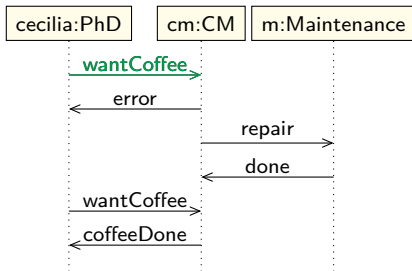
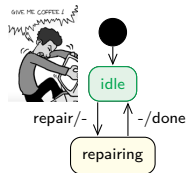
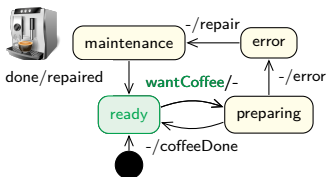
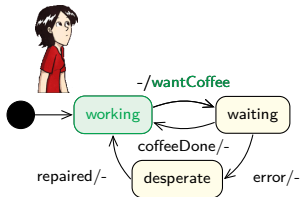
Sequence Diagram



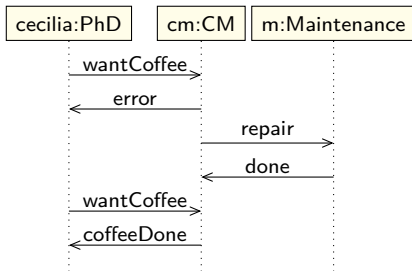
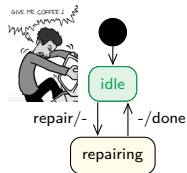
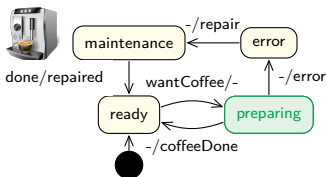
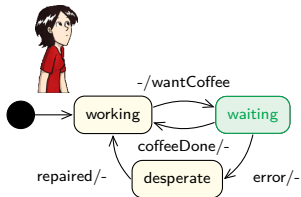
Sequence Diagram



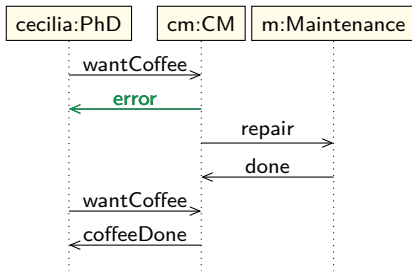
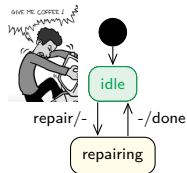
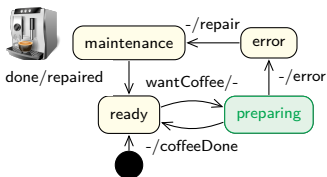
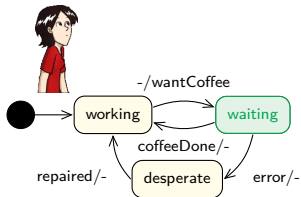
Sequence Diagram



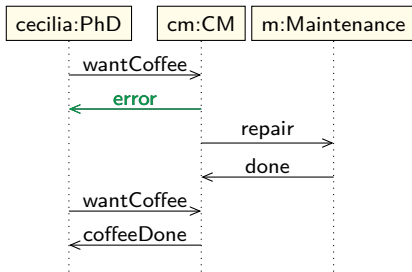
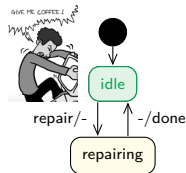
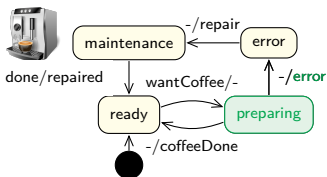
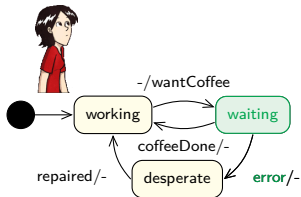
Sequence Diagram



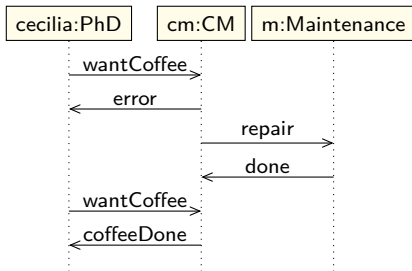
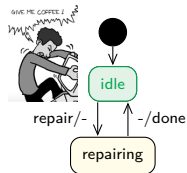
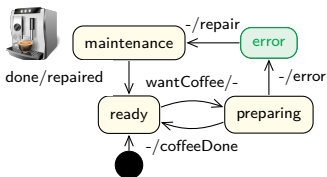
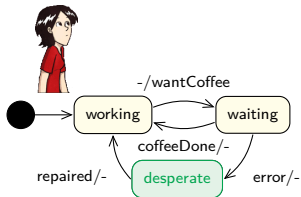
Sequence Diagram



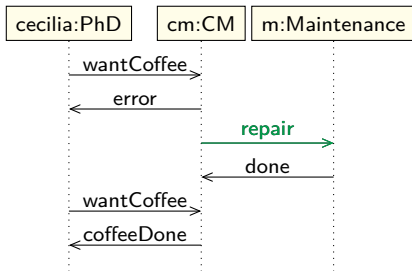
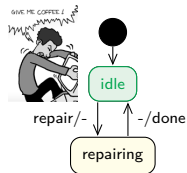
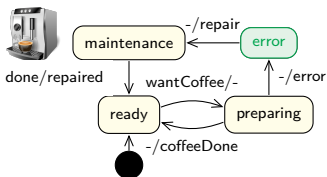
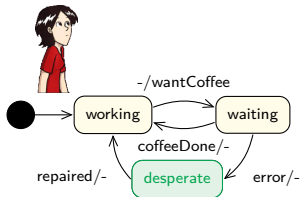
Sequence Diagram



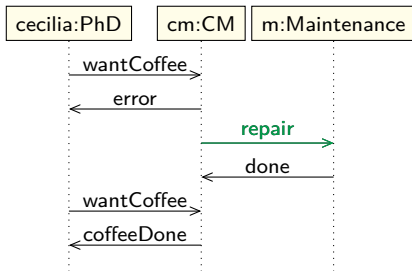
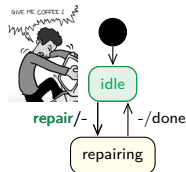
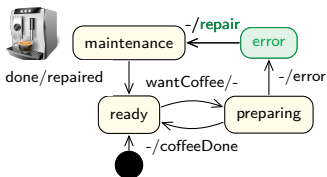
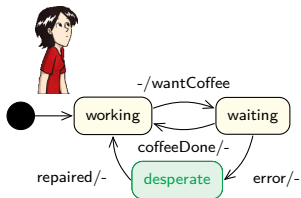
Sequence Diagram



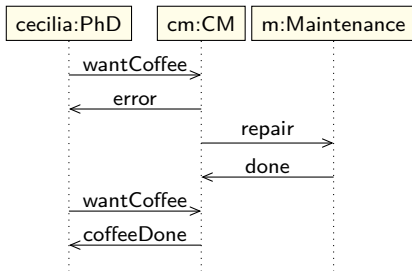
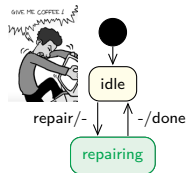
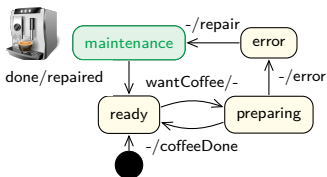
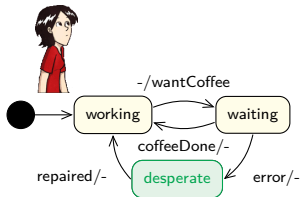
Sequence Diagram



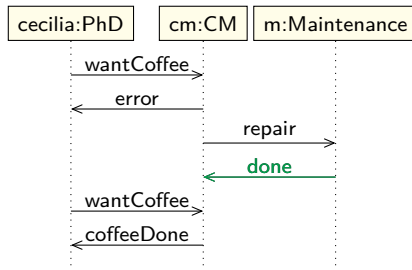
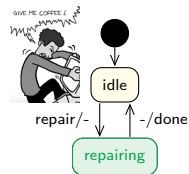
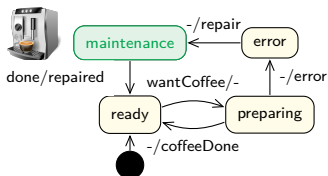
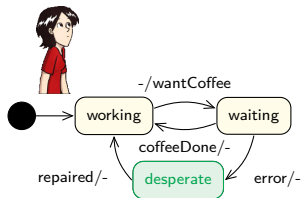
Sequence Diagram



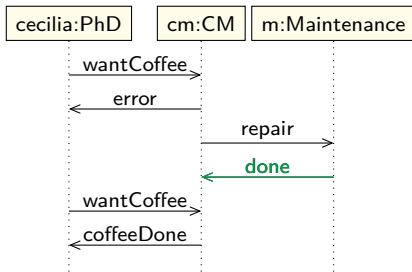
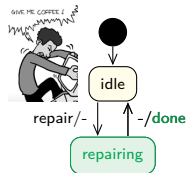
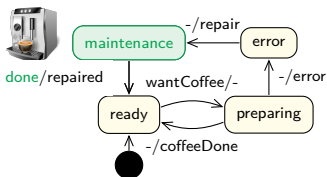
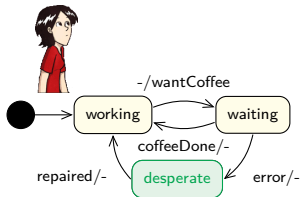
Sequence Diagram



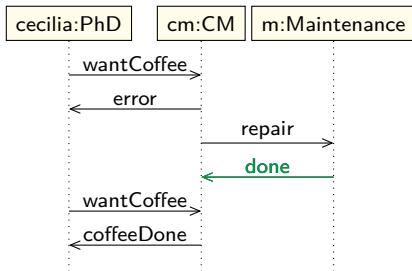
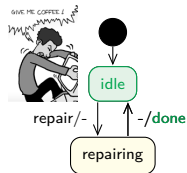
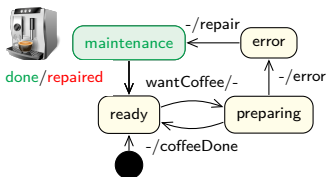
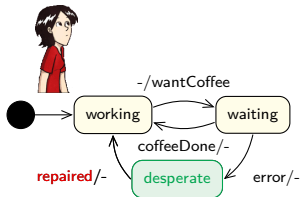
Sequence Diagram



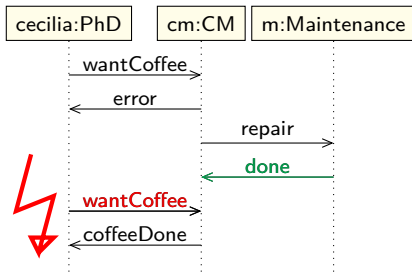
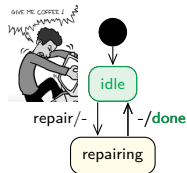
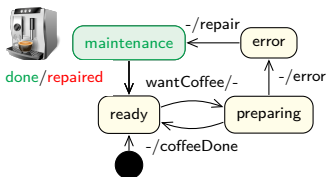
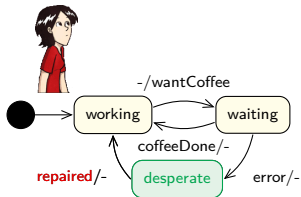
Sequence Diagram



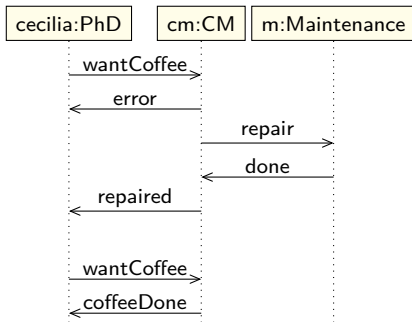
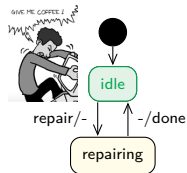
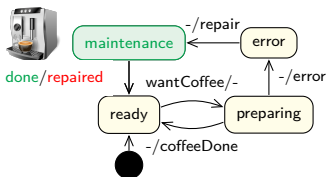
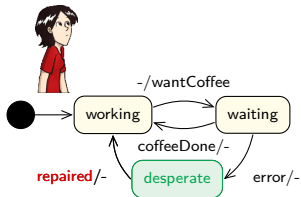
Sequence Diagram



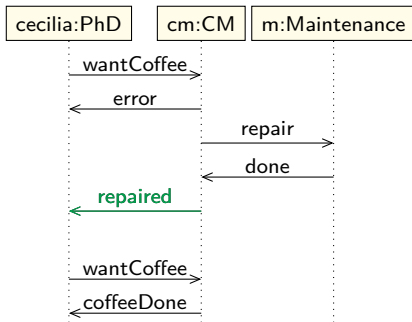
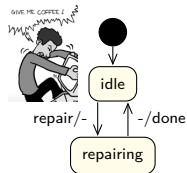
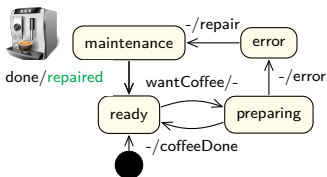
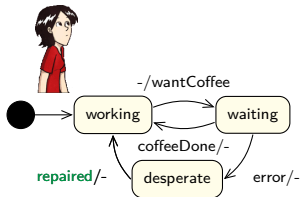
Sequence Diagram



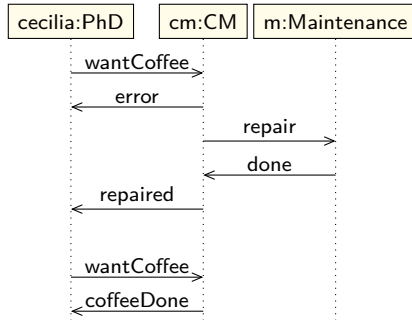
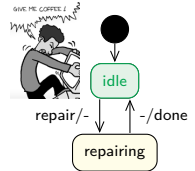
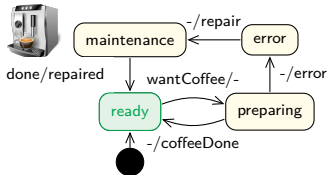
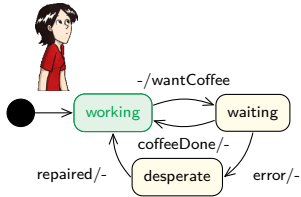
Sequence Diagram



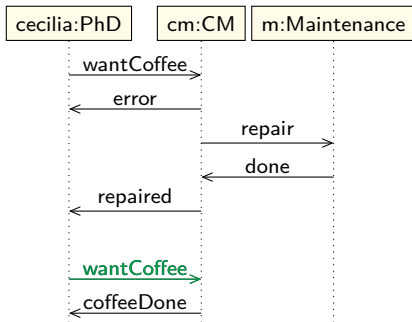
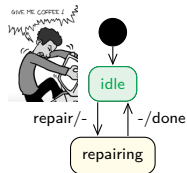
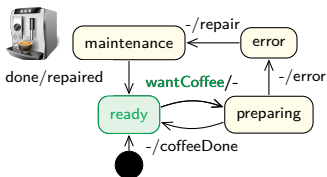
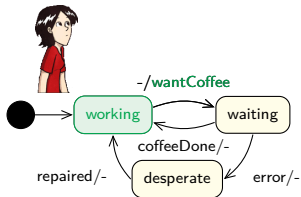
Sequence Diagram



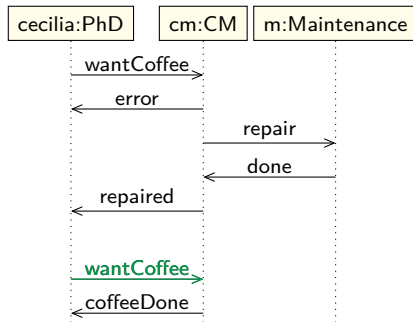
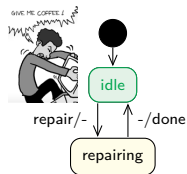
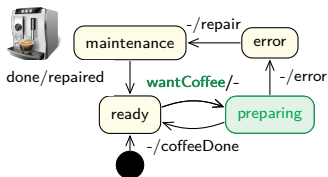
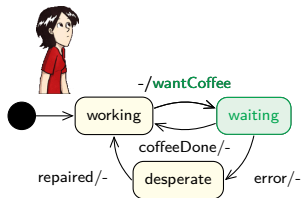
Sequence Diagram



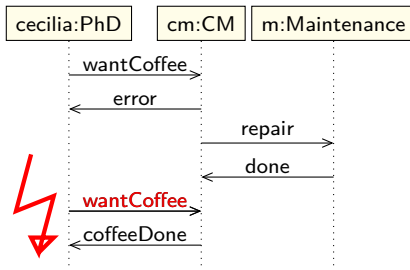
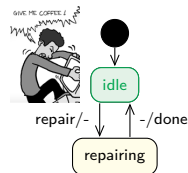
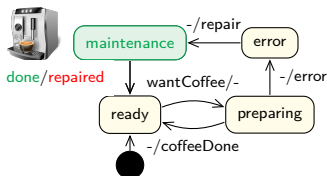
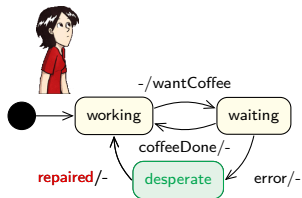
Sequence Diagram



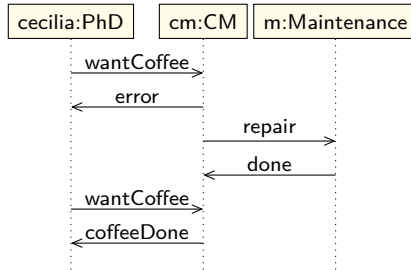
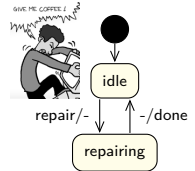
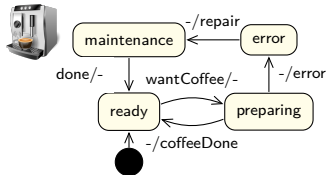
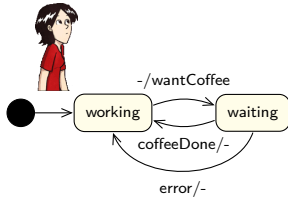
Sequence Diagram



Sequence Diagram



Sequence Diagram



The Problem

Check whether a sequence diagram is consistent with a set of state machines: Can the sequence diagram be executed (not necessarily from the initial states)?



The Problem

Check whether a sequence diagram is consistent with a set of state machines: Can the sequence diagram be executed (not necessarily from the initial states)?

Why not use a **model checker**?



The Problem

Check whether a sequence diagram is consistent with a set of state machines: Can the sequence diagram be executed (not necessarily from the initial states)?

Why not use a **model checker**?

Semantic differences!



The Problem

Check whether a sequence diagram is consistent with a set of state machines: Can the sequence diagram be executed (not necessarily from the initial states)?

Why not use a **model checker**?

Semantic differences!

Direct encoding to **SAT**



Propositional Satisfiability (SAT)



Propositional Satisfiability (SAT)

Instance: Propositional formula φ .

Question: Is there a satisfying truth assignment for φ ?



Propositional Satisfiability (SAT)

Instance: Propositional formula φ .

Question: Is there a satisfying truth assignment for φ ?

Example

$$\varphi = (x_1 \vee \overline{x_2}) \wedge (\overline{x_1} \vee x_3)$$

φ satisfiable?



Propositional Satisfiability (SAT)

Instance: Propositional formula φ .

Question: Is there a satisfying truth assignment for φ ?

Example

$$\varphi = (x_1 \vee \overline{x_2}) \wedge (\overline{x_1} \vee x_3)$$

φ satisfiable? Yes! For example: $x_1 = x_3 = \text{true}$, $x_2 = \text{false}$.



Propositional Satisfiability (SAT)

Instance: Propositional formula φ .

Question: Is there a satisfying truth assignment for φ ?

Example

$$\varphi = (x_1 \vee \overline{x_2}) \wedge (\overline{x_1} \vee x_3)$$

φ satisfiable? Yes! For example: $x_1 = x_3 = \text{true}$, $x_2 = \text{false}$.

- SAT solvers are very powerful – they handle millions of variables.
- Using SAT as a “programming language” is very successful.



Propositional Satisfiability (SAT)

Instance: Propositional formula φ .

Question: Is there a satisfying truth assignment for φ ?

Example

$$\varphi = (x_1 \vee \overline{x_2}) \wedge (\overline{x_1} \vee x_3)$$

φ satisfiable? Yes! For example: $x_1 = x_3 = \text{true}$, $x_2 = \text{false}$.

- SAT solvers are very powerful – they handle millions of variables.
- Using SAT as a “programming language” is very successful.

Use SAT for our problem!



Encoding

Variables

Variables representing **transitions** at positions:

t^i



Encoding

Variables

Variables representing **transitions** at positions:

$$t^i$$

Variables representing **message symbols** at positions:

$$eff^i, tr^i, \text{trg}(t)^i, a^i, \text{symb}(m)^i$$



Encoding

Variables

Variables representing **transitions** at positions:

$$t^i$$

Variables representing **message symbols** at positions:

$$eff^i, tr^i, trg(t)^i, a^i, symb(m)^i$$

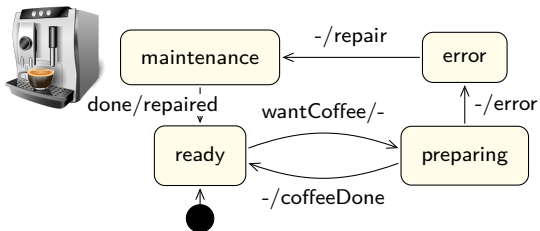
Variables representing **states** at positions:

$$src(t)^i, tgt(t)^i, int(t)^i$$



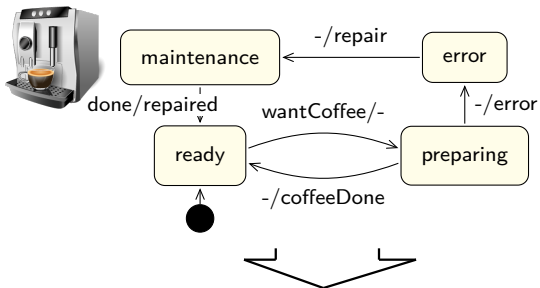
Encoding

Extended State Machine



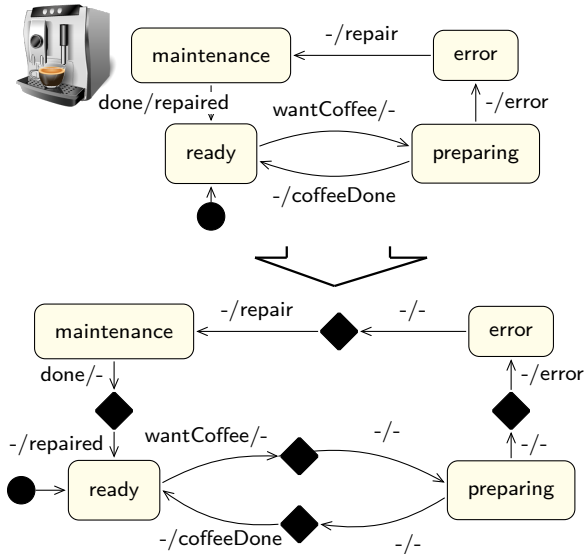
Encoding

Extended State Machine



Encoding

Extended State Machine



Encoding

Subformulas

- Initial state

$$\bigwedge_{i=1}^l \left(\iota_i^0 \wedge \bigwedge_{s \in S_i \cup S_i^*, s \neq \iota_i} \bar{s}^0 \right) \wedge \bigwedge_{a \in \mathcal{A}} \bar{a}^0$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{t \in \mathcal{T}} \left[t^i \rightarrow \left(\text{src}(t)^i \wedge \text{int}(t)^{i+1} \wedge \text{trg}(t)^i \wedge \overline{\text{trg}(t)}^{i+1} \wedge \bigwedge_{\text{eff} \in \text{eff}(t)} \left(\overline{\text{eff}}^i \wedge \text{eff}^{i+1} \right) \right) \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{trg \in \mathcal{A}} \left[trg^i \wedge \overline{trg}^{i+1} \rightarrow \bigvee_{t \in \mathcal{T}, trg = \text{trg}(t)} t^i \right]$$
$$\bigwedge_{i=0}^{k'-1} \bigwedge_{eff \in \mathcal{A}} \left[\overline{eff}^i \wedge eff^{i+1} \rightarrow \bigvee_{t \in \mathcal{T}, eff \in \text{eff}(t)} t^i \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes
- Leaving a state is caused by a transition

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{s \in S} \left[s^i \wedge \bar{s}^{i+1} \rightarrow \bigvee_{t \in \mathcal{T}, s = \text{src}(t)} t^i \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes
- Leaving a state is caused by a transition
- Consume symbol to finish transition

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{t \in \mathcal{T}, \text{eff}(t) \neq \epsilon} \left[(\text{int}(t)^i \wedge \text{int}(t)^{i+1}) \rightarrow \text{eff}(t)^{i+1} \right]$$

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{t \in \mathcal{T}, \text{eff}(t) \neq \epsilon} \left[\left(\text{int}(t)^i \wedge \overline{\text{int}(t)^{i+1}} \right) \rightarrow \overline{\text{eff}(t)^{i+1}} \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes
- Leaving a state is caused by a transition
- Consume symbol to finish transition
- Every machine is in exactly one state at every time

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{j=1}^l \left[\left(\bigvee_{s \in (S_j \cup S_j^*)} s^i \right) \wedge \bigwedge_{\substack{s_1, s_2 \in (S_j \cup S_j^*), \\ s_1 \neq s_2}} (\overline{s_1}^i \vee \overline{s_2}^i) \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes
- Leaving a state is caused by a transition
- Consume symbol to finish transition
- Every machine is in exactly one state at every time
- Move to target state when effect is consumed

$$\bigwedge_{i=0}^{k'-1} \bigwedge_{t \in \mathcal{T}} \left[\left(\text{int}(t)^i \wedge \bigwedge_{\text{eff} \in \text{eff}(t)} \overline{\text{eff}}^{i+1} \right) \rightarrow \left(\overline{\text{int}(t)}^{i+1} \wedge \text{tgt}(t)^{i+1} \right) \right]$$



Encoding

Subformulas

- Initial state
- State changes after initiating a transition
- There must be a cause whenever the polarity of a symbol changes
- Leaving a state is caused by a transition
- Consume symbol to finish transition
- Every machine is in exactly one state at every time
- Move to target state when effect is consumed
- Sequence diagram

$$\bigwedge_{\substack{i \in [1, \dots, n], \\ j \in [k, k+4, \dots, k+4n]}} \left[\text{symb}(m_i)^j \wedge \overline{\text{symb}(m_i)^{j+1}} \wedge \bigvee_{\substack{t \in \text{trans}(\text{snd}(m_i)), \\ \text{eff}(t) = m_i}} \left(\text{int}(t)^j \wedge \overline{\text{int}(t)^{j+1}} \right) \wedge \right. \\ \left. \bigwedge_{\substack{a \in \mathcal{A} \\ a \neq m_i}} \left((a^j \rightarrow a^{j+1}) \wedge (a^{j+1} \rightarrow a^{j+2}) \wedge (a^{j+2} \rightarrow a^{j+3}) \right) \right]$$



Encoding

Interpretation

Satisfiable: Message sequence computed from logical model



Encoding

Interpretation

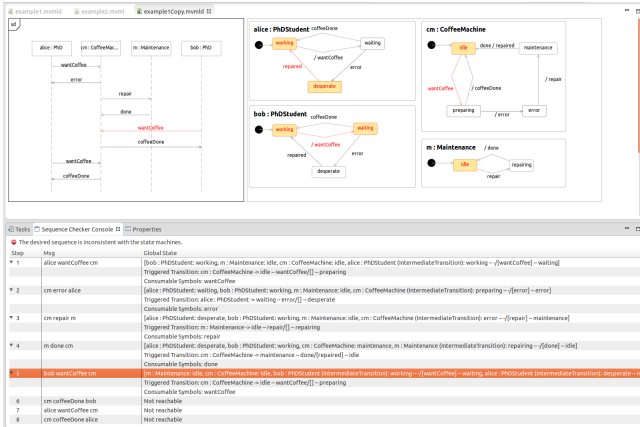
Satisfiable: Message sequence computed from logical model

Unsatisfiable: Sequence diagram cannot be executed



Implementation

- Multiview Modeling Language (MVMLL), inspired by UML
- Based on Ecore and EMF
- Graphical modeling editor



Download at <http://modelevolution.org/updatesite>



Evaluation

Random model generator



Evaluation

Random model generator

Different categories according to size

	small	medium	large
minNrStates	2	4	7
maxNrStates	3	6	10
minNrTrans	4	8	21
maxNrTrans	6	12	30
nrLifelines	3	5	8
nrMessages	4	10	20



Evaluation

Random model generator

Different categories according to size

	small	medium	large
minNrStates	2	4	7
maxNrStates	3	6	10
minNrTrans	4	8	21
maxNrTrans	6	12	30
nrLifelines	3	5	8
nrMessages	4	10	20

	small	medium	large
Encoding time <i>satisfiable</i> (ms)	11	180	2,543
Solving time <i>satisfiable</i> (ms)	4	201	9,476
Encoding time <i>unsatisfiable</i> (ms)	34	970	27,848
Solving time <i>unsatisfiable</i> (ms)	8	727	179,914
Nr variables	1,802	12,746	88,560
Nr clauses	9,652	118,245	1,700,101
Nr instances <i>satisfiable</i>	837	750	803
Nr instances <i>unsatisfiable</i>	163	250	197



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available
- Thorough evaluation



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available
- Thorough evaluation

What we consider next



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available
- Thorough evaluation

What we consider next

- Tuning and optimizing of the encoding



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available
- Thorough evaluation

What we consider next

- Tuning and optimizing of the encoding
- Additional language concepts requiring more complex encodings



Summary and Future Work

We presented

- SAT-based theoretical framework to check consistency between sequence diagrams and state machines
- Implementation, freely available
- Thorough evaluation

What we consider next

- Tuning and optimizing of the encoding
- Additional language concepts requiring more complex encodings
- More powerful target languages such as quantified Boolean formulae

